QUANTIFYING ERROR IN VEGETATION MAPPING

A Thesis presented to the Faculty of the Graduate School at the University of Missouri-Columbia

In Partial Fulfillment of the Requirements for the Degree Master of Sciences

by
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The undersigned, appointed by the dean of the Graduate School, have examined the thesis entitled

QUANTIFYING ERROR IN VEGETATION MAPPING

Presented by Erica Serna,

a candidate for the degree of master of Forestry,

and hereby certify that, in their opinion it is worthy of acceptance.

________________________________________
Professor Hong He

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Professor Daniel Dey

________________________________________
Professor John Fresen
Thank you Jesus Christ, Holy Spirit, and Father
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QUANTIFYING ERROR IN VEGETATION MAPPING

Erica Serna
Drs. Hong He, Daniel Dey and John Fresen, Thesis Advisers

Abstract

Understanding the current distribution and structure of forest vegetation is important for designing forest management plans and prioritizing restoration at landscape scales. This project provides information on Random Forest, a relatively new statistical package in the field of forestry, and patterns in mapping errors, a less explored field of study particularly in the forests of the Midwest United States. Vegetation maps can be made from classification and regression trees, such as Random Forest, by integrating environmental variables with vegetation information. An understanding of the accuracy of the maps is important because management plans and restoration efforts are more effective with accurate data. This study was done in forested regions in Minnesota with the purpose of 1) analyzing physiographic factors controlling tree species distribution; 2) mapping potential species distributions; 3) quantifying error in vegetation mapping; and 4) understanding map accuracy by evaluating minimum amounts of sample data necessary for reliable mapping. The results from Random Forest were found to be realistic ecologically and biologically. Also, tree species required records of 1-2 trees per 10,000 ha to produce accurate maps. Knowing the minimum amount of data points necessary for acceptable accuracy assists scientists mapping vegetation. This study demonstrates the effectiveness of Random Forest in vegetation mapping, which can be useful for future vegetation mapping.
Chapter 1

MAPPING TREE SPECIES DISTRIBUTIONS USING FOREST INVENTORY DATA AND ENVIRONMENTAL VARIABLES

Introduction

Understanding the current distribution and structure of forest vegetation is important for designing forest management plans and prioritizing restoration at landscape scales (Mladenoff, White, Pastor, & Crow, 1993). Humans have severely altered North American forests, including the boreal and northern hardwood forests in Minnesota, through decades of harvest, fire suppression, and other anthropogenic land uses (Friedman & Reich, 2005). Restoring these altered forests requires a landscape scale mapping assessment of current forest composition and structure.

Forest inventories provide the vegetation information to describe current conditions. A major source of forest inventory data nationally is the Forest Inventory and Analysis database administered by the USDA Forest Service (Data and Tools, 2010). The FIA database contains inventory plots distributed across the nation that have various parameters ranging from individual tree level information to the entire 0.4 hectare field plot (Forest Inventory and Analysis Program, 2008).
Researchers often use the FIA data in assessing and monitoring the nation’s forest ecosystem health, though the point data has two fundamental limitations. First, FIA data are at a density of 1-2 plots/10 km². The distance between points is generally too far for a typical ecological restoration task that is often conducted at individual sites less than a square kilometer in size. Second, point data is limiting in depicting spatially continuous vegetation (He, et al., 2007). GIS and spatial inference are often needed to convert point data into spatially continuous data forms. With additional environmental variables, spatial inference can also be effective in interpolating data from coarse resolutions to fine resolutions by determining vegetation in locations that data were not recorded.

Besides forest field inventories, researchers use remote sensing as another common vegetation mapping method at the regional and landscape scale (Jensen, 2000). Remote sensing is effective in capturing vegetation distribution but has limitations such as the inability to detect understory species (He, Mladenoff, Radeloff, & Crow, 1998; Stenback & Congalton, 1990). This prevents an accurate description of the forest structure and species composition.

Scientists have developed statistical models that integrate environmental variables with forest inventory plots to derive vegetation maps at fine resolutions and over large areas (Cutler, et al., 2007). Linear models, such as logistic regression, are often used in vegetation mapping by determining linear combinations of predictor variables to classify the data (Cutler, et al., 2007). Linear models limit accuracy in
mapping by the removal of correlating variables, which hinders interactions between variables to be expressed (Miller, Turner, Smithwick, Dent, & Stanley, 2004).

Classification and regression trees, such as Random Forest (RF), are a nonparametric alternative to the often inadequate linear models in modeling ecological data (De'ath & Fabricius, 2000). Classification trees develop rules for partitioning observations into two or more classes using predictor variables (Cutler, et al., 2007). The partitioning creates branches resulting in a tree-like appearance, hence the name classification tree. Random Forest exceeds the use of other common classification and regression methods in ecology (Cutler, et al., 2007; Prasad, Iverson, & Liaw, 2006) because the classification accuracy is high, it does not overfit the data and is very stable to small perturbations in the data (Cutler, et al., 2007). Other advantages include the ability to input missing values and determine variable importance.

**Objectives**

The first objective of this project is to analyze physiographic factors controlling tree species distribution. The second objective is to predict and map potential distributions of individual tree species based on the identified relationships between tree species and physiographic factors.

**Study Area**

According to the United States Forest Service (USFS) National Hierarchical Framework of Ecological Units, the study area includes a section of the Laurentian Mixed Forest (LMF) province in Minnesota (MN) as shown in Appendix A (Avers, et al.,
This landscape was selected because forests are the dominant vegetation type and because there are differences in common tree species that vary with the environment.

The LMF province covers 9.3 million hectares of the northeastern region of MN. Rolling to steep ridges, low bedrock knobs, peatlands and glacial lake plains dominate the landscape (Albert, 1995). The average elevation is between 200 and 400 meters above sea level. Annual precipitation ranges from 53 cm in the western portion of the region to 81 cm in the east. Vegetation is influenced by the low precipitation in the winter. The climate is characterized by short, mild summers with a mean temperature of 18°C and long, cold winters with a mean of -11°C. The soils are mainly alfisols, entisols and histisols (Albert, 1995). Conifer and hardwood-conifer forests dominate the province with species such as quaking aspen (Populus tremuloides), black spruce (Picea mariana) and balsam fir (Abies balsamea). Black spruce is most abundant according to FIA records (50%), followed by quaking aspen (13%), balsam fir (6%), and paper birch (Betula papyrifera) (5.7%).

Methods

Data Preparation

The Forest Service updates the FIA database containing tree data across the US every five to ten years. Forest Service employees collected the data for this project between 2000 and 2004. Field crews used fixed-radius plot layouts for sample tree selection in ground plots 0.4 ha in size. Across the landscape, the plot density is 1-2
plots/10 km². For more information on FIA sampling design, please refer to the FIA manual (Miles, et al., 2001). Due to privacy laws, the Forest Service fuzzed and swapped the exact plot locations (Lister, et al., 2005). All coordinates were fuzzed within 1.6 km of the exact plot location while most were within 0.8 km. Also, up to 20% of the private plot coordinates were swapped with similar private plots in the same county (Forest Inventory and Analysis Program, 2008). A Forest Service employee overlaid the accurate FIA data and prepared environmental data to produce accurate site conditions for tree species while maintaining privacy for private landowners.

The Natural Resources Conservation Service (NRCS) provides county level soil information available across the nation at mapping scales between 1:12,000 and 1:63,360 through the Soil Survey Geographic (SSURGO) Database. Limitations include error from digitizing the soil maps, which were hand drawn and unrepeatable. Also, the surveys are time consuming and done infrequently. The NRCS has not completed the SSURGO database in the entire LMF province, so the study area is only a portion of the province, where the soil survey has been completed. Five environmental variables were selected from SSURGO to predict tree distributions: available water capacity, organic matter, pH, and percent sand and clay. These covariates were selected because (1) they influence the basic needs of vegetation (e.g. sunlight, water and nutrients), (2) they were available in the study area (NRCS), and (3) they are relatively stable over time, and it is better to include more variables than necessary because Random Forest hierarchically determines the importance of each variable. All SSURGO calculations were at the map unit level, which contain one to three soil components each. All
environmental variables, including the raster data calculated at a resolution between thirty and sixty meters, were generalized to the SSURGO map unit level for determining potential species distributions.

Digital elevation models (DEM) were used at thirty meter resolution to calculate the topographic position index (TPI), topographic convergence (wetness) index (TCI), terrain ruggedness, mean slope in percent, aspect (transformed) in degrees and elevation for each SSURGO polygon. A sixty meter DEM was used to calculate solar radiation index due to the computation limitation.

These twelve environmental variables from SSURGO and DEMs are chosen to reflect the three main types of influences on species: limiting factors, disturbances and resources (Guisan & Thuiller, 2005). Though no actual disturbance variable is used, like fire frequency, this influence is accounted for by other variables like terrain ruggedness since highly rugged terrains typically have less disturbance than non-rugged terrains (Guyette, Spetich, & Stambaugh, 2006). Also, locations with high water availability have little disturbance. Random Forest statistical package performs best with quantitative data so qualitative variables like anthropogenic and natural disturbances were not used.

The TPI and TCI tools were downloaded from the Environmental Systems Research Institute (ESRI) website in a toolbox called Topography Tools written by Thomas Dilts (ESRI SUPPORT CENTER). The TPI categorizes raster cells into topographic position (i.e. ridge top, valley bottom, mid-slope, etc.) by finding the difference between a cell elevation value and the average elevation of the neighborhood around that cell.
Positive values mean the cell is higher than its surroundings while negative values indicate the cell is lower. Significantly higher values than the surrounding neighborhood indicate the cell is likely at or near the top of a hill or ridge. Significantly lower values suggest the cell is at or near the bottom of a valley. Values near zero could mean either a flat area or a mid-slope area. The TCI quantifies topographic control on soil moisture by calculating the upslope contribution area in hectares in relation to slope in percent by the equation

\[ TCI = \ln\left(\frac{a}{\tan \beta}\right) \]

where \( a \) is the upslope contribution and \( \beta \) is the local slope angle. Locations with high topographic convergence accumulate water more than areas with low convergence.

The terrain ruggedness was calculated with a vector ruggedness measure (VRM) for use in GIS written by Mark Sappington (Sappington M., 2008). The script is available through the ESRI website. The VRM utilizes the heterogeneity of slope and aspect in the dispersion of vectors in three dimensions (Sappington, Longshore, & Thompson, 2007). Values in the output raster range from 0 (no variation in the terrain) to 1 (complete variation). Natural terrains typically range between 0 and 0.4.

ESRI provided all other needed calculation tools within the GIS software ArcMap® version 9.3 (Environmental Systems Research Institute, 2008). Aspect was transformed using the equation

\[ A = \sin(A_1 + 45) + 1, \]

where \( A \) is the transformed aspect and \( A_1 \) is the original aspect in azimuth degrees (Trimble & Weitzman, 1956). A value of zero is equivalent to southwest.
After calculating all the environmental variables from raster data, the results were joined to the SSURGO data and generalized to the map unit level. All twelve environmental variables were then at a resolution equal to the SSURGO map unit.

Similar species were combined into the following species groups: ash, elm, maple, populus, red oak, spruce and white oak (Appendix B). The ash group contains black ash (*Fraxinus nigra*) and green ash (*Fraxinus pennsylvanica*). The elm group contains American elm (*Ulmus americana*) and slippery elm (*Ulmus rubra*). The maple group comprises red maple (*Acer rubrum*), silver maple (*Acer saccharinum*) and sugar maple (*Acer saccharum*). The populus group comprises balsam poplar (*Populus balsam*), bigtooth aspen (*Populus grandidentata*) and quaking aspen (*Populus tremuloides*). The red oak group contains northern pin oak (*Quercus ellipsoidalis*) and northern red oak (*Quercus rubra*). The spruce group contains white spruce (*Picea glauca*) and black spruce (*Picea mariana*). The white oak group comprises white oak (*Quercus alba*) and bur oak (*Quercus macrocarpa*).

The species groups were partitioned into three spatial patterns, aggregately, sparsely and widely distributed species based on species habit and current MN distribution (Appendix B). The aggregated species include jack pine (*Pinus banksiana*), northern white cedar (*Thuja occidentalis*), tamarack (*Larix laricina*) and white pine (*Pinus strobus*). The sparsely distributed species include the elm group, the red oak group, red pine (*Pinus resinosa*) and the white oak group. The widely distributed species
include American basswood (*Tilia Americana*), the ash group, balsam fir, the maple group, paper birch, the populus group and the spruce group.

**Spatial modeling**

Random Forest in R® statistical software was used for determining presence probability of species distribution (R Development Core Team, 2009). Random Forest was selected for this study because of the very high classification accuracy, and its ability to determine variable importance while performing statistical analyses like regression and classification. Another important feature of Random Forest for this study is the algorithm for imputing missing values.

Random Forest classifies observations by recursive binary partitioning into regions that are increasingly homogeneous (Breiman, 2001). Each classification tree that is created has ending branches called nodes. The tree is fully grown when further subdivision no longer reduces the Gini index (Cutler, et al., 2007). A difference between Random Forest and other classification trees is that Random Forest trees are not pruned once fully grown (Breiman, 2001). Many trees are grown from the data set and the predictions from all trees are combined to produce more accurate classifications.

Random Forest grows multiple trees by drawing bootstrap samples with in-bag observations (typically 63% of the data points are selected to develop trees) and out-of-bag observations (the unused data points to calculate error and variable importance later). Bagging increases accuracy when randomizing methods are used (Breiman, 2001). Each bootstrap sample grows one tree and at each node only a small amount of
randomly selected variables are used to grow the individual branches. Often the number of variables is the square root of the total amount of variables used. The random and small amount of variables at each node ensures that correlations among the grown trees are small (Cutler, et al., 2007). The fully grown trees are used to predict the out-of-bag observations, performing a cross-validation of the results.

Fifteen maps, one for each species, were created based on the FIA tree data and prepared environmental variables using Random Forest. The FIA data provides tree species presence information and the environmental variables provide information on relevant site conditions which Random Forest uses to predict probability of tree presence. The Random Forest results were imported into ArcMap® to create the fifteen individual species group maps (Environmental Systems Research Institute, 2008).

The accuracy and error rates were computed for each observation using the out-of-bag predictions, and the results simplified by averaging all observations creating a kind of cross-validation of accuracy estimates without needing a set aside data set (Cutler, et al., 2007). Sixty three percent of the inputs were used for modeling and 37% for the validation. Cross-validation creates bias without a known extent but the out-of-bag estimates are unbiased (Breiman, 2001). In Random Forest, each tree is given a misclassification rate according to the out-of-bag observations. Then the values of the predictor variables are randomly altered for the out-of-bag data and pass through the tree to get new predictions. To determine the importance value of a variable, the
difference between misclassification rates (original and altered out-of-bag data) are divided by the standard error (Cutler, et al., 2007).

The results from Random Forest were joined to a Minnesota map in ArcMap to create presence probability maps. These maps display probability classes as follows: 0-0.25, 0.25-0.5, 0.5-0.75 and 0.75-1.

The map results were compared to the FIA known present locations using the receiver operating characteristic (ROC) package called ROCR in R statistical software to quantify the accuracy of each map. A curve is created that is a graphical plot of the sensitivity of the system when the value considered truly present from the Random Forest presence probability results is varied. This is done by plotting the true positive rate against the false positive rate. The true positive rate is the fraction of presences found in the FIA data and the Random Forest results out of the total presences from the FIA data. The false positive rate is the fraction of FIA locations without a species present that Random Forest predicted as present to the total absences from the FIA data. A true positive rate of 1 would imply that Random Forest perfectly classified each location where a species was present in the FIA data.

**Results**

**Predicted potential species distribution**

The widely distributed species that Random Forest predicted include American basswood, the ash group, balsam fir, the maple group, paper birch, the populus group and the spruce group (Figures 1-6). The most important variables for American basswood include topographic convergence index (TCI), terrain ruggedness, also known
as vector ruggedness measure (VRM), and clay. American basswood is most frequently found in a TCI around 5.16, VRM of $3 \times 10^{-4}$ and percent clay around 12% (Figure 1). For the ash group, Random Forest found percent sand and aspect to be the most important variables. Ash is most frequently found in percent sand near 5% or 48% and a NW aspect (Figure 2). Ash is representative of a species with a wide distribution. This species group can be found throughout the study area, beyond the north-central area where there is a high density of high probability polygons. Solar radiation index, organic matter (OM) and elevation are most important for balsam fir. Balsam fir is most frequently found when SRI is near 5483 Watt hours per square meter (WH/m$^2$), OM is 7.2% and at elevations around 417 m (Figure 3). For the maple group, Random Forest found TCI and aspect to be the most important variables. Maples are typically found when TCI is around 5.0 and on NW aspects (Figure 4). The probability potential of paper birch occurrence is best predicted using TCI, solar radiation index (SRI), and elevation (Figure 5). Paper birch is most frequently found when TCI is near 5.1, SRI averages 5483 WH/m$^2$ and at elevations of 419 m. The most important variables for the populus group include TCI and SRI. Populus species are most frequently found when TCI is around 5.2 and SRI is 5487 WH/m$^2$ (Figure 6). The spruce group is best predicted according to Random Forest by OM and percent sand. The highest probabilities of occurrence for spruce occur when OM is near 10 percent and percent sand is 5 (Figure 7).

The aggregated species groups that Random Forest predicted include jack pine (Figure 8), northern white cedar (Figure 9), tamarack (Figure 10) and white pine (Figure 11). For jack pine, Random Forest found percent sand and clay to be the most important
variables. Jack pine is typically found in areas of 90% sand and 4% clay. Jack pine is a good representative of aggregated species because of the clumps of high probability polygons. Most polygons are aggregated as opposed to isolated. Percent OM and aspect are the most important predictor variables for northern white cedar. Northern white cedar is most frequently found when OM is near 9.5% and on NW aspects. The most important variables for tamarack include OM, slope and TCI. Tamarack is most frequently found in soils with 10% OM, on gentle (1.3%) slopes and where TCI is 6.5. White pine is best predicted according to Random Forest by TCI, sand and slope. White pine corresponds to a TCI value of 5.0, 71% to 93% sand and 3.7% slope.

The sparsely distributed species that Random Forest predicted include the elm group (Figure 12), the red oak group (Figure 13) and red pine (Figure 14). The pH and SRI are the most important predictor variables for the elm group. The elm group is most frequently found in a pH of 6.5 and an SRI near 5476 WH/m². For the red oak group, Random Forest found the VRM, TCI and slope to be the most important variables. The red oak group is typical of a VRM of 0.000401, TCI near 5.0 and a slope around 1.7%. The most important variables for red pine include sand and available water capacity (AWC). Red pine corresponds with soils with 87% sand and 0.032 cm/cm AWC and is typical of sparsely distributed species. The majority of the landscape has less than 50% probability of containing red pine and only a small portion with larger than 75% probability. Large, aggregated sections of the study area do not show red pine as potentially present.
Random Forest created a map of the white oak group distributed widely throughout the study area when it is a sparsely distributed species group (Figure 15). White oaks are generalists and are sprinkled throughout the range in varying densities, making it difficult for Random Forest to map. The most important variables for the white oak group include TCI and OM. The white oak group is most frequently found in a TCI near 5.18 and OM around 1.06%.

The northern white cedar had the highest true positive rate (TPR) at 0.96, which is near perfect classification (Table 2). The American basswood, jack pine, red pine and tamarack are also at or above 0.90. All of the aggregately distributed species, except for white pine, have the highest TPR values. Balsam fir and the spruce group have TPR values of 0.88. The ash, maple, red oak and white oak groups also have TPR values above 0.80. Paper birch, the populus group and white pine have TPR values in the 0.70 to 0.79 range and elm has the lowest TPR at 0.63. These TPR values are based on a 0.75 cutoff, where all Random Forest presence probabilities above 0.75 are considered present.
Table 1 Importance value results produced by RF for the ten most important variables for each species group. Random Forest assigned how important each variable was for predicting the presence probability for each species.

<table>
<thead>
<tr>
<th>Species Group</th>
<th>Most Important</th>
<th>Least Important</th>
</tr>
</thead>
<tbody>
<tr>
<td>basswood</td>
<td>TCI 0.821, VRM 0.806, Clay 0.789, Aspect 0.738, AWC 0.734, Sand 0.726, Slope 0.702, OM 0.763, TPI 0.673, Elevation 0.665</td>
<td></td>
</tr>
<tr>
<td>ash</td>
<td>Sand 0.72, Aspect 0.691, Slope 0.688, TCI 0.654, Elevation 0.64, TPI 0.639, OM 0.576, Clay 0.568, AWC 0.636, SRI 0.636</td>
<td></td>
</tr>
<tr>
<td>balsam fir</td>
<td>SRI 0.818, OM 0.815, Elevation 0.785, pH 0.699, TCI 0.684, VRM 0.673, Clay 0.665, Sand 0.662, Aspect 0.649, Slope 0.626</td>
<td></td>
</tr>
<tr>
<td>maple</td>
<td>TCI 0.711, Aspect 0.688, Slope 0.63, VRM 0.617, Sand 0.613, Elevation 0.522, SRI 0.482, Clay 0.465, TPI 0.463</td>
<td></td>
</tr>
<tr>
<td>paper birch</td>
<td>TCI 0.693, SRI 0.68, Elevation 0.647, Slope 0.633, VRM 0.535, Aspect 0.517, OM 0.478, Sand 0.449, pH 0.437</td>
<td></td>
</tr>
<tr>
<td>populus</td>
<td>TCI 0.853, SRI 0.633, Elevation 0.564, Aspect 0.555, Clay 0.525, Sand 0.513, OM 0.513, AWC 0.502, TPI 0.495</td>
<td></td>
</tr>
<tr>
<td>spruce</td>
<td>OM 0.837, Sand 0.787, Slope 0.742, VRM 0.68, Aspect 0.608, OM 0.593, SRI 0.401, Clay 0.373, TPI 0.373</td>
<td></td>
</tr>
<tr>
<td>jack pine</td>
<td>Sand 0.605, Clay 0.478, TCI 0.431, VRM 0.412, Sand 0.396, OM 0.301, AWC 0.3, TPI 0.247, OM 0.186</td>
<td></td>
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<tr>
<td>cedar</td>
<td>OM 0.885, Aspect 0.615, Slope 0.564, VRM 0.517, Sand 0.482, AWC 0.461, TPI 0.427, OM 0.426, VRM 0.411</td>
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<tr>
<td>tamarack</td>
<td>OM 0.795, Slope 0.743, TCI 0.696, VRM 0.487, Sand 0.461, AWC 0.42, SRI 0.385, Clay 0.36, TPI 0.282</td>
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<tr>
<td>white pine</td>
<td>TCI 0.63, Slope 0.625, Sand 0.578, VRM 0.577, TCI 0.57, OM 0.531, AWC 0.51, SRI 0.474, TCI 0.454</td>
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<tr>
<td>elm</td>
<td>pH 0.943, SRI 0.863, Elevation 0.861, Clay 0.836, OM 0.785, AWC 0.784, Aspect 0.784, Sand 0.754, TCI 0.722</td>
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<tr>
<td>red oak</td>
<td>TCI 0.989, VRM 0.849, Slope 0.634, TPI 0.629, Aspect 0.589, Sand 0.586, AWC 0.551, OM 0.538, VRM 0.525</td>
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<tr>
<td>red pine</td>
<td>Sand 0.823, VRM 0.781, Slope 0.734, TPI 0.69, Aspect 0.672, Sand 0.573, AWC 0.538, OM 0.519, SRI 0.513</td>
<td></td>
</tr>
<tr>
<td>white oak</td>
<td>TCI 0.987, OM 0.828, Elevation 0.792, SRI 0.705, Slope 0.682, Sand 0.652, TPI 0.61, AWC 0.609, OM 0.513</td>
<td></td>
</tr>
</tbody>
</table>
Figure 1 Probability classes for potential American basswood occurrence

Figure 2 Probability classes for potential ash group occurrence

Figure 3 Probability classes for potential balsam fir occurrence

Figure 4 Probability classes for potential maple group occurrence
Figure 5 Probability classes for potential paper birch occurrence

Figure 6 Probability classes for potential populus group occurrence

Figure 7 Probability classes for potential spruce group occurrence

Figure 8 Probability classes for potential jack pine occurrence
Figure 9 Probability classes for potential northern white cedar occurrence

Figure 10 Probability classes for potential tamarack occurrence

Figure 11 Probability classes for potential white pine occurrence

Figure 12 Probability classes for potential elm group occurrence
Figure 13 Probability classes for potential red oak group occurrence

Figure 14 Probability classes for potential red pine occurrence

Figure 15 Probability classes for potential white oak group occurrence
Table 2 True positive rate for each species from the ROCR package in R statistical software.

<table>
<thead>
<tr>
<th>Species</th>
<th>True Positive Rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>basswood</td>
<td>0.90</td>
</tr>
<tr>
<td>ash</td>
<td>0.82</td>
</tr>
<tr>
<td>balsam fir</td>
<td>0.88</td>
</tr>
<tr>
<td>maple</td>
<td>0.84</td>
</tr>
<tr>
<td>paper birch</td>
<td>0.78</td>
</tr>
<tr>
<td>populus</td>
<td>0.74</td>
</tr>
<tr>
<td>spruce</td>
<td>0.88</td>
</tr>
<tr>
<td>jack pine</td>
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</tr>
<tr>
<td>cedar</td>
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</tr>
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<td>tamarack</td>
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<td>white pine</td>
<td>0.76</td>
</tr>
<tr>
<td>elm</td>
<td>0.63</td>
</tr>
<tr>
<td>red oak</td>
<td>0.83</td>
</tr>
<tr>
<td>red pine</td>
<td>0.93</td>
</tr>
<tr>
<td>white oak</td>
<td>0.83</td>
</tr>
</tbody>
</table>

Discussion

The results from Random Forest for widely distributed species (American basswood, ash, balsam fir, maple, paper birch, poplar, aspen and spruce) are supported by the species habitat characteristics. American basswoods are large, rapid growing trees found in deep moist soils (Fowells, 1965). They are shade tolerant. Random Forest predicted presence probability the highest in moist soils and low variations in terrain.

Black and green ashes grow in moist soil areas. They are shade intolerant, early successional species. Random Forest predicted the highest probability in sandy soils, that occur near streams (Burns & Honkala, 1990). There is also high probability of ash in sand at only 5%, typical of peats, bogs and lakes. Ashes are also predicted to grow on NW facing slopes, providing cool and moist soils.
Balsam firs are small to medium size trees that are very shade tolerant (Burns & Honkala, 1990; Bergeron, 2000). Soil moisture is an important environmental factor to the species, which explains Random Forest considering solar radiation the most important predictor variable. Higher incoming solar radiation dries out soils and lower amounts of solar radiation can provide an environment for cool and moist soils.

Maples grow on a wide variety of sites and are very shade tolerant (Allen, Molloy, Cooke, & Pendrel, 1999). Optimum growth is on soils that are not too wet and not too dry. They are not fire tolerant but grow well after disturbance. Random Forest predicted presence probability the highest in average to low TCI values compared to other species and slopes with a NW aspect, suggesting that shaded locations are more favorable for maples.

Paper birches are medium-sized, fast-growing trees found on almost any soil and topographic position, which are characteristics of species that have low mapping accuracy (Guisan, et al., 2007). They are shade intolerant and have thin bark (Bergeron, 2000; Burns & Honkala, 1990). Paper birch is predicted in similar locations to balsam fir but more wide spread.

Balsam poplar, bigtooth aspen and quaking aspen are early successional species found in floodplains. They are fast growing, shade intolerant and medium-sized trees (Huffman, Fajvan, & Wood, 1999). Random Forest predicted the highest probability in sunny and moist locations, like river bottoms.
Black and white spruces are found in a wide range of edaphic and climatic conditions. They are intermediate in tolerance to shade (Bergeron, 2000; Fowells, 1965). Spruces do not grow well in sandy soil which is supported by Random Forest by predicting spruces in about 5% sand locations.

The aggregated species (jack pine, northern white cedar, tamarack and white pine) are logically mapped by Random Forest according to previously known habitat characteristics of the tree species. The high true positive rate (TPR) values of the aggregately species, except for white pine, also demonstrate the accuracy of Random Forest predictions (Table 2). Jack pines are small to medium-sized, very shade intolerant trees that invade areas after major disturbances (Bergeron, 2000). They can grow on very dry, sandy soils that are inhospitable to other species but grow best on well drained loamy sands. Red pines often succeed jack pines on loamy sand soils, followed by white pine, then hardwoods such as sugar maple, basswood and northern red oak. Paper birch and quaking aspen frequently succeed jack pine instead of red and white pine, followed by the hardwoods or a spruce-fir association (Burns & Honkala, 1990). Random forest found percent sand and clay to be the most important variables and predicted highest probability of jack pines in 90% sand soils.

Northern white cedar is a shade tolerant and found in the northeastern part of MN (Bergeron, 2000). It grows most commonly on cool, moist, organic soils like near streams and drainage-ways (Burns & Honkala, 1990). Random Forest assigned OM and aspect as most important variables supporting previously known habitat characteristics.
of northern white cedar. The preferable NW aspect provides the cool and moist environment on which the cedars thrive.

Tamaracks are small to medium-sized deciduous conifers that are very shade intolerant. They can tolerate a wide range of edaphic conditions but are most commonly found in moist, organic soils (Burns & Honkala, 1990). Tamaracks can grow in more extreme sites like peatlands. Random Forest correctly identified moisture and organic matter to be important variables with tamarack having higher probability of presence in organic, moist locations.

White pines are intermediate in shade tolerance and associated with somewhat excessively drained sandy deposits (Burns & Honkala, 1990). They can survive in soils with a pH value as low as 4.0 and are climax species in these extreme sites. Random Forest predicted highest probability of white pines on sandy, steep slopes. White pine has a low TPR value suggesting that the Random Forest model is not as strong for this species as it is for other species even though the previously known habitat characteristics of the tree species align with the Random Forest results.

The results from Random Forest for sparsely distributed species (elm, red oak and red pine) are supported by the species habitat characteristics. Elms are intermediate in shade tolerance and exist in a pH range of 5.5 to 8.0 (Fowells, 1965). In MN, elms are associated with plains, moraine hills, bottomlands and swamp margins. They can be found a variety of soils like well drained sands to poorly drained clays. Dutch elm disease has severely decreased the amount of American elms leaving a small
percentage of large diameter trees in mixed forest stands. Random Forest predicted elm at a mean pH of 6.5 and also found the average amount of solar radiation in MN suitable for elms. Even with the correlation between the species habitat characteristics and the Random Forest results, elm had the lowest TPR value (0.63) suggesting that the model used was not sufficient for mapping this species.

Northern red oak and northern pin oak grow on a wide range of soils and topography which proves more difficult to map than species that grow in narrow niches. Red oaks are intermediate in shade tolerance and often form pure stands. Random Forest considers lightly rough terrains on slopes with a TCI of 5.0 to be the most important environmental variables for mapping. Previous research determined aspect, slope position and shape to be important variables for red oaks (Burns & Honkala, 1990).

Red pines are medium-sized trees that are shade intolerant. They grow best on sandy soils adjacent to bodies of water. Due to changes in land management and timber harvesting, red pine populations declined drastically in previous decades (Leahy & Pregitzer, 2003). Random forest found percent sand to be the most important variable and predicted highest probability of red pines in 87% sand soils.

White oaks and bur oaks are very drought resistant and often dominate severe sites like thin soils, claypans and gravel ridges (Burns & Honkala, 1990). They are intermediate in shade tolerance and are often replaced by maple-basswood communities. Random Forest mapped the white oak group as widely distributed in the
study area when it is a sparsely distributed species group. One reason may be most of
the land has a potential for white oaks according to the variables used to create the
model. White oaks do not out-compete other species, like maples, well in colder
climates like northern MN. A climate variable, like temperature, would be a good
addition for predicting species distributions.

In summary, the predictions from Random Forest are realistic ecologically
because the locations that were predicted to have high probability of presence align
with the species biological and ecological attributes. Also, the important variables
chosen by Random Forest align with the species known attributes.

A suggestion for future research is including weather variables to see if species,
like white oak, are mapped more ecologically realistic. Another suggestion would be to
use a different statistical approach, other than a CART, and adding disturbance variables
like type of disturbance (fire, clearcut, shelterwood) and frequency of the disturbance.
Chapter 2

QUANTIFYING ERROR IN TREE SPECIES MAPPING

Introduction

Species maps are often used in management planning and restoration projects. Accurate estimates of species distributions are required to create effective management and restoration projects. The modeling of the species distribution is an important tool in the area of conservation (Guisan & Zimmermann, 2000).

Many statistical methods have been developed to compare created maps to data assumed to be true (Engler, Guisan, & Rechsteiner, 2004). The comparison can be done between forest inventory plots and a vegetation map, or between two vegetation maps. A comparison between point data and a vegetation map has limitations due to the lack of overlapping data. On the other hand, it is difficult to acquire an accurate vegetation map to which one can compare a second vegetation map.

To determine the accuracy of created maps, Kappa statistics have been used frequently in previous studies, though many have not differentiated between location and quantity errors (Pontius, 2000; Congalton, 1999). The Kappa statistic was found to be the most useful statistic for determining agreement between maps in previous research (Monserud & Leemans, 1992). Specific knowledge of the source of error,
location or quantity, can better assist the user in understanding map accuracy.

Limitations to the Kappa statistic include an assumption that the data samples are independent, which is not always true in vegetation mapping since the created maps are often derived from the same data set (Leeuw, et al., 2006).

Other similar cross-tabulation methods based on locations throughout a map have been used (Foody, 2007). McNemar’s test is based on a chi-square statistic. The null hypothesis states that the proportion of pixels will be correctly classified in both maps (Leeuw, et al., 2006). A limitation of McNemar’s test is that the variable must be dichotomous. Explained deviance calculates the percentage of deviance but is limited to goodness of fit for generalized linear models (Finos, Brombin, & Salmaso, 2010). The receiver-operating characteristic plot method (ROC) creates a curve that is a graphical plot of the sensitivity of the system when the value considered truly present is varied. The ROC has the advantage of being threshold-independent but has limitations in models that do not have predictions across the entire study area (Peterson, Papes, & Soberon, 2008).

Mapping species with different spatial distribution patterns and life history characteristics can have diverse mapping accuracies (Guisan, et al., 2007). Species with high mapping accuracy include dominant, slow-growing species with narrow geographic distributions and that are good competitors (Guisan, et al., 2007). Also, species with contiguous distributions map more accurately (Reese, Wilson, Hoeting, & Flather, 2005). Conversely, early successional species that are rarely dominant and often scattered
among other species prove more difficult to map (Guisan, et al., 2007). Map accuracy can be affected by the spatial pattern of tree species distributions, such as aggregately, sparsely and widely distributed patterns. Understanding mapping accuracy is critical for the end user who will use the map for management plans.

The amount of data points used to create a vegetation map affects the accuracy of the map. Using larger sample sizes improves model performance (Reese, Wilson, Hoeting, & Flather, 2005). Guisan, et al. (2007) found that larger sample sizes produce more accurate results and that each species varies greatly in necessary data points, even within each tree genus.

Many studies have been done to determine the minimum amount of data required to create an accurate map, particularly for animals. In multiple studies, as low as 10 data points in a landscape scale have been found to be sufficient for mapping species (Hernandez, Graham, Master, & Albert, 2006; Wisz, et al., 2008). Hernandez, et al. (2006) studied insects, birds and mammals in California. Wisz, et al. (2008) studied a variety of animals and plant species around the globe. The results of the mobile and non-mobile species were comparable with as low as 10 data points necessary for accurate mapping. Kadmon, Farber, and Danin (2003) found 50 data points (a density of about 0.18 trees per 10,000 ha) to be sufficient for accurate mapping of woody vegetation in Israel.

This study aims to research the minimum data points necessary for mapping common tree species. Different maps were created in the study area for each tree
species by using varying amounts of tree data. These maps were then compared to
determine the accuracy of each map. Comparing the similarity in location of categorical
information and the quantity of locations with each category between two maps can be
used to quantify map accuracy.

**Objectives**

The first objective of this project is to quantify error in vegetation mapping
based on the common species distribution patterns, aggregately, widely and sparsely
distributed. The second objective is to understand map accuracy by evaluating minimum
amounts of sample data necessary for reliable mapping.

This project provides information on patterns in mapping errors, a less explored
field of study particularly in the forests of the Midwest United States. Also, a fairly new
technology in the forestry field was used, Random Forest statistical package, to gain
more accurate results than in previous research. Random Forest is a nonparametric
alternative to the often inadequate linear models in modeling ecological data (De'ath &
Fabricius, 2000). Linear models, such as logistic regression, are often used in vegetation
mapping by determining linear combinations of predictor variables to classify the data
(Cutler, et al., 2007). Linear models limit accuracy in mapping by the removal of
correlating variables, which hinders interactions between variables to be expressed
(Miller, et al., 2004).

Random Forest exceeds the use of other common classification and regression
methods in ecology (Cutler, et al., 2007; Prasad, Iverson, & Liaw, 2006) because the
classification accuracy is high, it does not overfit the data and is very stable to small perturbations in the data (Cutler, et al., 2007). More accurate maps and an understanding of the limitations of a map can aid in designing forest management plans and in prioritizing large scale restoration.

The tree species in the study area have diverse distributions and spatial patterns. The differences in mapping accuracy were determined between three spatial patterns in tree species distributions, aggregately, sparsely and widely distributed. Based on a set of unique site characteristics, presence probability maps in the Laurentian Mixed Forest (LMF) province in Minnesota were produced. Various amounts of data points were used for each species to generate a set of maps and compared individual map predictions among all maps for that species using kappa statistics. Knowing the minimum amount of data points necessary for acceptable accuracy will help scientists mapping vegetation. Separating the species into spatial patterns provides a more specific number of points tailored to individual species.

**Study Area**

According to the United States Forest Service (USFS) National Hierarchical Framework of Ecological Units, the study area includes a section of the Laurentian Mixed Forest (LMF) province in Minnesota (MN) as shown in Appendix A (Avers, et al., 1994). This landscape was selected because forests are the dominant vegetation type and because there are differences in common tree species in the environment.
The LMF province covers 9.3 million ha of the northeastern region of MN. Rolling to steep ridges, low bedrock knobs, peatlands and glacial lake plains dominate the landscape (Albert, 1995). The average elevation is between 200 and 400 meters above sea level. Annual precipitation ranges from 53 cm in the west to 81 cm in the east of the province. Vegetation is influenced by the low precipitation in the winter. The climate is characterized by short, mild summers with a mean temperature of 18°C and long, cold winters with a mean of -11°C. The soils are mainly alfisols, entisols and histisols (Albert, 1995). Conifer and hardwood-conifer forests dominate the province with species such as quaking aspen (Populus tremuloides), black spruce (Picea mariana) and balsam fir (Abies balsamea). Black spruce grows most abundantly according to FIA records (50%), followed by quaking aspen (13%), balsam fir (6%), and paper birch (Betula papyrifera) (5.7%).

**Methods**

Chapter 1 discusses the data preparation and creation of maps using the maximum amount of data points available in the study area. After creating a map for each species using the maximum amount of data points for the model in Random Forest, maps were produced with successively less data points. Seventy five percent of the total data points were used, then fifty percent, followed by twenty five percent. Also, two more sets of maps were created using different amounts of data points to find the minimum amount necessary to create accurate maps for each species by predicting the minimum based on results from the 75%, 50% and 25% trials. Amounts used can be found in Appendix C.
Random Forest produces a table including species presence probability for each SSURGO polygon. In ArcMap the table that Random Forest produced based on the maximum data points available was joined to the MN SSURGO shapefile. Then the 75% data point prediction table was also joined to the shapefile. Each polygon in the shapefile has two probability categories, one for the maximum data points and one for the 75%. These values were compared to determine the mapping accuracy. This process was repeated for the various trials of different data point amounts.

An error matrix was constructed to compare the maps of the same species with different sample amounts. From the matrix, Kno, Klocation and Khisto values were calculated to quantify error. Kappa is the amount of agreement between two maps after chance agreement has been removed ranging from -1, major difference, to 1, perfect similarity. Kno shows the proportion correctly classified in relation to the expected proportion classified correctly by a model with no ability to specify the quantity or location accurately (Pontius, 2000). Klocation and Khisto demonstrate the source of error, whether location or quantity. Klocation indicates the similarity in spatial distribution of categories but does not differentiate between categories that are close and categories that are distant and is independent of the total number of cells per category (Pontius, 2000). Values are similar to kappa except Klocation can go far below -1. Khisto is a measure of quantitative similarity between two maps (Hagen, 2002) and multiplying Khisto by Klocation yields kappa (Prasad, Iverson, & Liaw, 2006).
Kappa values between 0.81 and 1 represent almost perfect agreement, 0.61 to 0.8 represent substantial agreement, 0.41 to 0.6 represent moderate agreement, 0.21 to 0.4 represent fair agreement, 0 to 0.2 represent slight agreement and less than 0 represent poor agreement (Landis & Koch, 1977). Accurate maps are defined as having a K statistic above 0.61.

Another quantification error statistic, Kquantity (Pontius, 2000), is dependent on Klocation, defeating the purpose of separating quantity error from location error (Sousa, Caeiro, & Painho, 2002) and is not used in this study. Klocation and Khisto demonstrate the sources of error showing scientists where improvement is most needed (Pontius, 2000).

Each map is homogenous in species but produced from different data points and amounts. Species groups were partitioned into three spatial patterns, aggregately, sparsely and widely distributed species based on species habit and current MN distribution for further analysis (Appendix B). The aggregated species include jack pine, northern white cedar, tamarack and white pine. The sparsely distributed species include the elm group, the red oak group, red pine and the white oak group. The widely distributed species include American basswood, the ash group, balsam fir, the maple group, paper birch, the populus group and the spruce group.

Results

Comparison of prediction agreement
According to Kno, the aggregated species are mapped more accurately than the widely distributed species followed by the sparsely distributed species (Figure 16). The Kno displays four distinguished groups of accuracy, groups A\textsubscript{kno}, B\textsubscript{kno}, C\textsubscript{kno} and D\textsubscript{kno} (Figure 17). Group A represents the most accurate mapping and group D represents the least accurate. Group A\textsubscript{kno} consists of only aggregated species, group B\textsubscript{kno} and C\textsubscript{kno} contain aggregately, sparsely and widely, and group D\textsubscript{kno} contains only sparsely. The aggregated species produce maps with substantial agreement even with only 25% of the data points used in building the model. No other species attained this level of accuracy. Most species have a large drop in mapping accuracy after the data points used is below 50%, most likely because below 50% results in about 600 or less data points or 1.23 trees per 10,000 ha in the study area.

Klocation produced similar results. The aggregated species are mapped more accurately than the widely distributed species, followed by the sparsely distributed species (Figure 18). Group A\textsubscript{kloc} comprises aggregately and widely distributed species, group B\textsubscript{kloc} sparsely and widely, group C\textsubscript{kloc} aggregately, sparsely and widely, and group D\textsubscript{kloc} only sparsely distributed species (Table 3).

Khisto also shows that aggregated species are mapped more accurately than the widely distributed species, followed by the sparsely distributed species (Figure 19). Group A\textsubscript{kloc} has only aggregated species, group B\textsubscript{kloc} aggregated and widely, group C\textsubscript{kloc} aggregated, sparsely and widely, and group D\textsubscript{kloc} only sparsely distributed species (Table
4). Tamarack is found in group A for all three statistics while the elm group is found in group D for all three statistics (Figure 17, Table 3, and Table 4).

Sparsely distributed species require the fewest data points to produce accurate location maps. The widely distributed species require the most amount of data points, while aggregated species fall in the middle (Figure 20). Of the widely distributed species, the ash group and the populus group require 900 points or 1.84 trees per 10,000 ha, paper birch and the spruce group require 800 points or 1.63 trees per 10,000 ha, balsam fir and the maple group require 600 points or 1.23 trees per 10,000 ha and American basswood requires 400 points or 0.82 trees per 10,000 ha to map location accurately. Of the aggregated species, northern white cedar and tamarack require 700 points or 1.43 trees per 10,000 ha, jack pine requires 300 points or 0.61 trees per 10,000 ha and white pine requires 100 points or 0.20 trees per 10,000 ha. Of the sparsely distributed species, red pine requires 600 points or 1.23 trees per 10,000 ha and the elm group, the red oak group and the white oak group require 400 points or 0.82 trees per 10,000 ha to map accurately.

Random Forest mapped quantity better than location for all species and required fewer data points to accurately map quantity. As with the location maps, sparsely distributed species require the fewest points to produce accurate quantity maps. Aggregated species require the second fewest while widely distributed species require the most data points (Figure 21). The widely distributed species need between 400 and 700 points or 0.82 and 1.43 trees per 10,000 ha. The ash group, paper birch and the
The widely distributed species had the largest amount of data records in the FIA database and did not map accurately when building the model with less than 700 records or 1.43 trees per 10,000 ha. This brings into question the accuracy of the map for white pine because there are less than 700 records present in the database. The map considered real is merely created from the maximum records available, up to 2,500 records due to computer limitations.

Exact amounts of data points necessary to accurately map aggregately, sparsely or widely distributed species could not be determined due to the vast differences between species within each spatial pattern group. With a conservative approach, the largest minimum amount of points required in each spatial pattern can be considered the minimum (Table 5). For example, the ash group, a widely distributed species group,
requires 1,100 points or 2.25 trees per 10,000 ha to produce an accurate map according
to Kno so the minimum amount of data points for widely distributed species is 1,100.
The widely distributed species require more data points than sparsely and aggregated to
attain the same level of mapping accuracy. According to Kno, aggregated species require
700 points or 1.43 trees per 10,000 ha and sparsely require 500 points or 1.02 trees per
10,000 ha. To accurately map location, more data points are necessary than to
accurately map quantities of each category. Widely distributed species require a
minimum of 900 points or 1.84 trees per 10,000 ha to map location and 700 points or
1.43 trees per 10,000 ha to map quantity accurately. Aggregated species require 700
points or 1.43 trees per 10,000 ha for location and 350 points or 0.71 trees per 10,000
ha for quantity. Sparsely distributed species require 400 points or 0.82 trees per 10,000
ha for location and only 200 points or 0.41 trees per 10,000 ha to map quantity
accurately (Table 5).

Figure 16 Average Kno at each comparison level, 75%, 50% and 25% of total FIA points by each spatial pattern
group
Figure 17 Kno values for all 15 tree species broken into four distinct accuracy groups

Figure 18 Average Klocation value by spatial pattern group
Table 3 Groupings based on accuracy according to Klocation

<table>
<thead>
<tr>
<th>Group A</th>
<th>Group B</th>
<th>Group C</th>
<th>Group D</th>
</tr>
</thead>
<tbody>
<tr>
<td>balsam fir</td>
<td>maple group</td>
<td>ash group</td>
<td>elm group</td>
</tr>
<tr>
<td>American basswood</td>
<td>red oak group</td>
<td>white oak group</td>
<td></td>
</tr>
<tr>
<td>paper birch</td>
<td>red pine</td>
<td></td>
<td></td>
</tr>
<tr>
<td>jack pine</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>northern white cedar</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>populus group</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>spruce group</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>tamarack</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 19 Average Khisto by spatial pattern group

Table 4 Groupings by accuracy based on Khisto statistic

<table>
<thead>
<tr>
<th>Group A</th>
<th>Group B</th>
<th>Group C</th>
<th>Group D</th>
</tr>
</thead>
<tbody>
<tr>
<td>tamarack</td>
<td>balsam fir</td>
<td>ash group</td>
<td>elm group</td>
</tr>
<tr>
<td>white pine</td>
<td>maple group</td>
<td>American basswood</td>
<td></td>
</tr>
<tr>
<td>norhtern white cedar</td>
<td>red oak group</td>
<td>paper birch</td>
<td></td>
</tr>
<tr>
<td>spruce group</td>
<td>red pine</td>
<td>jack pine</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>populus group</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>red oak group</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>white pine group</td>
<td></td>
</tr>
</tbody>
</table>

Percent of total points used

Khisto value

0.00 0.20 0.40 0.60 0.80 1.00 1.20

Khisto value

75% 50% 25%

widely

aggregated

Sparsely

39
Figure 20 Amount of data points necessary to create accurate maps by species according to Klocation

Figure 21 Amount of data points necessary to create accurate maps by species according to Khisto

Table 5 Largest minimum density of species that each spatial pattern requires in trees per 10,000 ha

<table>
<thead>
<tr>
<th></th>
<th>Kno</th>
<th>Location</th>
<th>Quantity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Widely</td>
<td>2.25</td>
<td>1.84</td>
<td>1.43</td>
</tr>
<tr>
<td>Aggregately</td>
<td>1.43</td>
<td>1.43</td>
<td>0.71</td>
</tr>
<tr>
<td>Sparsely</td>
<td>1.02</td>
<td>0.82</td>
<td>0.41</td>
</tr>
</tbody>
</table>
Discussion

Quantifying error

Aggregated species mapped most accurately in both location and quantity. This was expected because dominant species have previously been found to have higher mapping accuracy and aggregated species often out-compete and become dominant in stands (Guisan, et al., 2007). Widely distributed species fell second in accuracy and sparsely were the least accurate. Widely distributed species were probably difficult to map because they do not have a narrow geographic distribution. They can be found on a variety of landscapes making it difficult for Random Forest to accurately predict presence probability. Sparsely distributed species are difficult to map because they are the minority in stands.

According to all three statistics, Kno, Kloc and Khisto, elm had the lowest mapping accuracy and tamarack had the highest accuracy. Elms are moderately fast growing species, which have been previously found to have lower mapping accuracy (Guisan, et al., 2007). Tamaracks often form pure stands making them the dominant trees in a stand. In mixed stands, tamaracks are in the overstory. Both characteristics are associated with high mapping accuracy.

Sparsely distributed species require the fewest data points to accurately map location. This may be caused by the fewer data points available to create the true map since the species is not as common as widely distributed species. Widely distributed species require the largest amount of data points to map location accurately. A potential
reason for this is the small fraction of the total data points used to create the model in Random Forest and an overwhelming amount of points to test the accuracy of the model. Two thirds of the data should be used to build the model but due to computer limitations, a maximum of 2,500 data points could be used. This is a small fraction of the 24,440 points of trees in the populus group, resulting in a sample taken from a sample which can lead the data farther from being an accurate representation of reality.

The ash group and populus group, both widely distributed, require the most points to map location accurately. White pine, aggregated distribution, requires the least amount of data points. The accuracy of white pine’s true map should be questioned because it was created with only 322 points at a density of 0.66 trees per 10,000 ha.

The quantity of polygons in each probability class mapped more accurately overall and with fewer data points than the location of each polygon when comparing the true map to the alternate maps with fewer data points used to build the model. As with location, sparsely distributed species required the fewest data points for quantity accuracy and widely distributed species required the most. Again the ash and populus groups require the most amount of data points while white pine requires the least. Paper birch is also among the species that require the largest amount of data points to map accurately.
Improving mapping accuracy

The creation of accurate species distribution maps needs a certain amount of data points. Each species is unique and has a different minimum amount of data points necessary. In this project, I attempted to determine the minimum amount necessary to create accurate maps using Random Forest based on the species distribution pattern. The results show that in general, widely distributed species require more data points, followed by aggregated then sparsely.

Widely distributed species had the most available data points to create the true map. It may be inferred that the widely distributed species true maps are the most accurate and it was found that the widely distributed species require a minimum of 1,100 points or 2.25 trees per 10,000 ha to maintain accuracy. Elm and white pine did not have 1,100 records in the study area.

This study produced a wide range of minimum data points within the three distribution groups making it difficult to determine a minimum amount necessary based on distribution pattern. According to the largest amount necessary of a species within each group, widely distributed species should have at least 1,100 points or 2.25 trees per 10,000 ha to produce an accurate map. Only 900 points or 1.84 trees per 10,000 ha are required to map location accurately and 700 points or 1.43 trees per 10,000 ha to map quantity accurately. Aggregated species require 700 points or 1.43 trees per 10,000 ha but if the user is only interested in quantity accuracy, only 350 points or 0.71 trees per 10,000 ha are required. Sparsely distributed species require 500 points or 1.02 trees
per 10,000 ha to map accurately according to Kno, 400 points or 0.82 trees per 10,000 ha for location accuracy and only 200 points or 0.41 trees per 10,000 ha for quantity accuracy.

Using larger sample sizes improves model performance (Reese, Wilson, Hoeting, & Flather, 2005) and with current technology, there is no need to decrease data with the goal of improving processing time. Kadmon, Farber, and Danin (2003) found 50 data points (a density of about 0.18 trees per 10,000 ha) to be sufficient for accurate mapping. In multiple studies, as low as 10 data points in a landscape scale have been found to be sufficient for mapping species (Hernandez, Graham, Master, & Albert, 2006; Wisz, et al., 2008). Guisan, et al. (2007) found that larger sample sizes produce more accurate results and that each species varies greatly in necessary data points, even within each tree genus. A limitation in this study may be in the grouping species together. Further studies should be done in Minnesota without grouping species to determine minimum data points necessary for accurate mapping.

Limitations in this study include relying solely on FIA data to demonstrate current tree species locations because of the spatial gaps in the FIA point data. Only species presence information was available. The absence of a species was not taken into account. Also, the environmental variables are at a coarse resolution and have heterogeneous environmental conditions within each map unit. The FIA plots are smaller than the map unit which may affect mapping accuracy. The model was developed using the observed distribution of tree species in relation to the calculated
environmental variables but is not extensive enough to describe all possible combinations of environmental variables. A model limitation can be seen in species like white oak, white pine and elm. The white oak species was expected to be sparsely distributed but Random Forest predicted it as a widely distributed species, white pine had very few data records in FIA and elm had the lowest Kappa values. A computer limitation occurred with large data sets, like the populus group. A sample of the FIA sample had to be taken, possibly leading the data set farther from an accurate representation of reality.

Suggestions for future research are including weather variables to see if species, like white oak, are mapped more ecologically realistic. Also, research should be done on why white oak was mapped as widely distributed and why elm had the lowest mapping accuracy. Future vegetation mapping projects could use a different statistical approach for the methodology of variable selection, regression and dealing with large data sets.
LITERATURE CITED


NRCS. SSURGO Metadata - Table Column Descriptions Version 2.2.3. USDA Natural Resource Conservation Service.


Appendix

Appendix A

Map of study area in the Laurentian Mixed Forest Province in Minnesota
## Appendix B

Tree species in the study for MN.

<table>
<thead>
<tr>
<th>Species</th>
<th>Species Group</th>
<th>Spatial Pattern</th>
</tr>
</thead>
<tbody>
<tr>
<td>Larix laricina</td>
<td>tamarack</td>
<td>aggregately</td>
</tr>
<tr>
<td>Pinus banksiana</td>
<td>jack pine</td>
<td>aggregately</td>
</tr>
<tr>
<td>Pinus strobus</td>
<td>white pine</td>
<td>aggregately</td>
</tr>
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<td>Thuja occidentalis</td>
<td>northern white cedar</td>
<td>aggregately</td>
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<td>Pinus resinosa</td>
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<td>Quercus rubra</td>
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</tr>
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<td>Ulmus rubra</td>
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<td>Tilia americana</td>
<td>American basswood</td>
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**Appendix C**

Amount of FIA data points used in each trial.

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<th>Maximum data points available</th>
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<th>50% of maximum data points</th>
<th>25% of maximum data points</th>
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