ASYMPTOTIC UNCONDITIONALITY IN BANACH SPACES

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ABSTRACT

We show that a separable real Banach space embeds almost isometrically in a space Y with a shrinking 1-unconditional basis if and only if $\lim_{n\to\infty} ||x^* + x_n^*|| =$ $\lim_{n\to\infty} ||x^* - x_n^*||$ whenever $x^* \in X^*$, $(x_n^*)_{n=1}^{\infty}$ is a weak*-null sequence and both limits exist. If X is reflexive then Y can be assumed reflexive. These results provide the isometric counterparts of recent work of Johnson and Zheng.